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# **Section 1: Basidiomycete Life-Style**

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# CHAPTER 1

## Mycelial Networks: Structure and Dynamics

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### Abstract

For continuing survival saprotrophic fungi must be able to capture organic resources discontinuously dispersed in space and time. Some Basidiomycota can only achieve this by production of sexual and asexual spores or sclerotia — categorized as 'resource-unit-restricted', whereas 'non-resource-unit-restricted' Basidiomycota can also spread between organic resources as mycelium. Mycelial distribution and foraging within organic resources and among relatively homogeneously and heterogeneously distributed resources is reviewed. 'Non-resource-unit-restricted' Basidiomycota have evolved different patterns of mycelial spread appropriate to discovery of resources of different sizes and distributions. They show remarkable patterns of re-allocation of biomass and mineral nutrients on discovery and colonization of new resources. Network architecture is a significant factor in the acquisition and distribution of nutrients, and in survival when parts of the network are destroyed. The costs and benefits of different architectures to large mycelial networks are considered.

## 1. INTRODUCTION

3 For most Basidiomycota in terrestrial ecosystems the predominant body form is  
4 the mycelium, comprising an interconnecting series of apically extending tubes  
5 —hyphae. Hyphae provide a large surface:volume, ideal for secreting enzymes  
6 for extracellular digestion of resources (Chapter 2), and for subsequent uptake of  
7 small molecules. Mineral nutrients, carbon and energy sources are presumed to  
8 be taken up largely at hyphal tips, be they embedded within an organic resource  
9 or foraging externally for new resources, and translocated from these sources to  
10 sites of demand (sinks; Chapter 3). Nutrient acquisition and other aspects of  
11 physiology are affected by the local environment (Chapter 2), and mycelia exhibit  
12 remarkable physiological and morphological plasticity. Moreover, since mycelial  
13 activity in one region can be supported by supply of water and nutritional re-  
14 sources from elsewhere, growth can sometimes occur in inhospitable places and  
15 adverse conditions. The interconnectedness of mycelia is of crucial significance to  
16 the organization and ecological roles of fungi (Rayner *et al.*, 1995).

17 In terrestrial ecosystems, the organic resources on which saprotrophic Bas-  
18 idiomycota depend are usually discrete, varying in size from small to large plant  
19 fragments, e.g. bud scales, leaves and large woody components. These resources  
20 are distributed heterogeneously in both space and time, for example, the rela-  
21 tively homogeneous carpet of forest floor leaf litter comprises spatially discrete  
22 leaves, input largely over a 6–8 week period in autumn by broadleaf deciduous  
23 trees, or more evenly during the year by many conifers. Branches are patchily  
24 distributed on the forest floor, falling throughout the year, though often with  
25 larger inputs following high winds. For continuing survival saprotrophic fungi  
26 must be able to capture these discontinuously dispersed resources. Some  
27 Basidiomycota can only achieve this by production of sexual and asexual spores  
28 or sclerotia, and have been categorized as ‘resource-unit-restricted’, whereas  
29 ‘non-resource-unit-restricted’ Basidiomycota can also spread between organic  
30 resources as mycelium. Spores, although allowing rapid spread, sometimes over  
31 long distances, contain only relatively small food reserves from which to produce  
32 a mycelium for invasion of the organic resource upon which it has landed.  
33 Sclerotia often provide larger resources and also allow survival in time. Growth  
34 as mycelium, in contrast, allows the fungus to draw upon a much larger supply  
35 of nutrients.

36 This chapter considers mycelia growing within organic resources, and the  
37 ways in which they search and colonize them when discontinuous. It also ex-  
38 amines the significance of network architecture, and the costs and benefits of  
39 large mycelial networks.

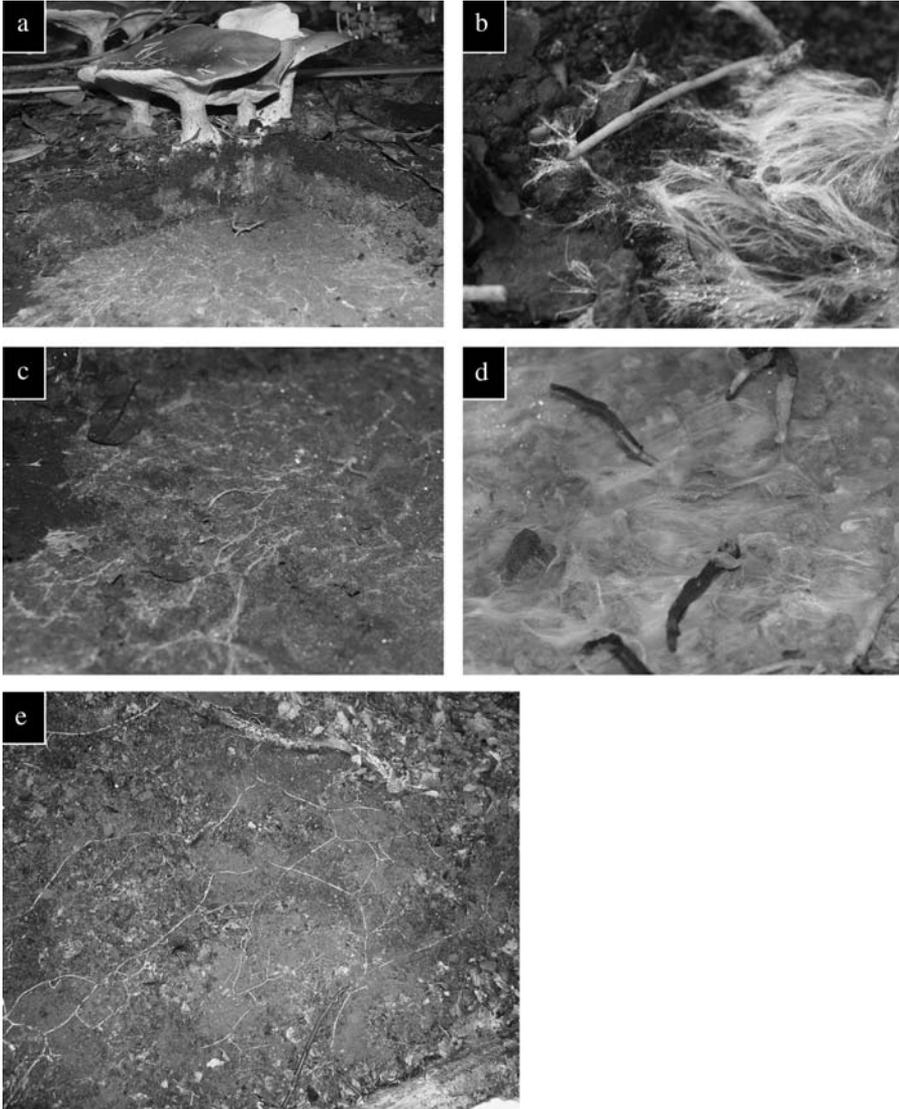
## 2. MYCELIA WITHIN ORGANIC SUBSTRATA

41 There is little information on mycelia within organic resources. Exceptions are  
42 maps of the extent of mycelia, inferred from interaction zone lines (see Chapters 7  
43  
44  
45

1 and 11), and location of hyphae in relation to type of rot (Rayner and Boddy,  
2 1988). The size of mycelia ranges from a few millimetres to many metres, in the  
3 case of longitudinally extensive (30 m or more) primary colonizers of attached  
4 branches and standing trunks (Boddy, 2001). The three-dimensional shape of the  
5 mycelial boundary is largely governed by the anatomy of the resource and by  
6 surrounding antagonistic fungi. For example, in wood, decay columns tend to be  
7 larger longitudinally than in other directions, reflecting difficulty of radial and  
8 tangential spreads. The diamond shaped cankers on sycamore (*Acer pseudoplat-*  
9 *anus*) caused by *Dichomera saubinetii* (Ascomycota) result from spread between  
10 nutrient rich ray cells (Bevercombe and Rayner, 1980). Crucially lacking, how-  
11 ever, is knowledge of the interconnectedness of different parts of the mycelium,  
12 and even the amount of mycelial biomass at different locations within organic  
13 resources. That there is spatial heterogeneity of mycelial distribution within  
14 wood decay columns is suggested by the common observation that when wood is  
15 incubated in a humid environment mycelium often grows out rapidly and pro-  
16 fusely from the edges, and more slowly and less densely from more central  
17 regions.

### 19 **3. MYCELIA FORAGING BETWEEN RELATIVELY HOMOGENEOUSLY** 20 **DISTRIBUTED RESOURCES**

23 Fungi have evolved a variety of foraging and behavioural responses to encoun-  
24 ters with new resources. Fungi that utilize individual, relatively homogeneous  
25 resources, e.g. a leaf litter layer, effectively colonize as if individual components  
26 are simply parts of a larger resource. Mycelia form large patches with no  
27 particular pattern, e.g. *Collybia* spp. and *Marasmius* spp., or form fairy rings, e.g.  
28 *Clitocybe nebularis* (Dowson *et al.*, 1989). Nothing is known of the network  
29 architecture of mycelial patches, but fairy rings of *C. nebularis* extend through the  
30 leaf litter layer as an ever increasing annulus of mycelium ~30–40 cm wide  
31 (Dowson *et al.*, 1989; Figure 1a–d). The band is differentiated into three distinct  
32 zones: (1) the leading edge comprises mycelial cords (linear organs of predom-  
33 inantly parallel hyphae) spreading across the leaf litter layer and up to 6 cm into  
34 soil beneath; (2) a central region of dense mycelium which ramifies throughout,  
35 and presumably causes, intensely bleached leaf litter but does not extend into the  
36 mineral soil; (3) mycelium at the trailing edge which becomes progressively  
37 fragmented before completely disappearing. (Fruit bodies are produced from the  
38 middle of zone 2.) This outwardly extending annulus does not form as a result of  
39 lack of nutrients in central areas, as these are replenished every autumn, nor are  
40 toxic metabolites likely to be the cause, since when part of the annulus was  
41 transplanted into this region it grew well (Dowson *et al.*, 1989). Rather, these  
42 mycelia exhibit highly polarized growth, such that when a turf containing all  
43 zones of the annulus was relocated elsewhere, growth continued in the original  
44 direction of travel with limited lateral growth (Dowson *et al.*, 1989). Young  
45 mycelia of *C. nebularis* form patches, but what triggers annulus formation is



37 **Figure 1 (a–d)** Mycelium of a *Clitocybe nebularis* Fairy Ring which had Developed under a  
 39 Paving Slab in a Garden. (a) Location of Fruit Bodies in Relation to Mycelium. Note  
 41 Aggregation into Cords, but still with Diffuse Mycelium, towards the Leading Edge (Left). (b)  
 Mycelium Aggregating into Fine Cords at Leading Edge. (c) Thicker Cords amidst Dense Fine  
 Mycelium. (d) Very Dense, Fine Mycelium in Central Zone of Annulus. (e) Mycelial Network of  
*Megacollybia platyphylla* in a Mixed Deciduous Woodland, Revealed by Removal of Surface  
 Litter. Digital Images (a)–(d) Courtesy of David Moore.

43 unknown. Presumably ring formation is related to size and might be expected to  
 45 start when a patch is over 80 cm diameter (i.e. double the width of the mycelial  
 band).

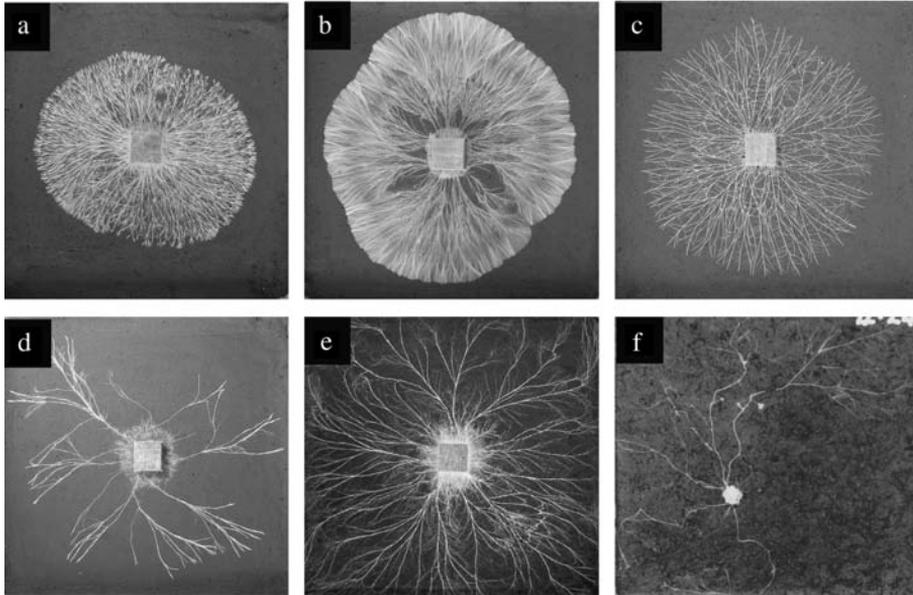
## 4. MYCELIA FORAGING BETWEEN RESOURCES DISTRIBUTED HETEROGENEOUSLY IN SPACE AND TIME

Fungi that utilize spatially discrete resources, with centimetre- or even metre-scale separations, have developed a variety of foraging strategies. They commonly form linear mycelial aggregates termed rhizomorphs, e.g. *Marasmius androsaceus* and *Armillaria* spp., or cords, e.g. *Hypholoma fasciculare* and *Phanerochaete velutina* (e.g. Boddy, 1984, 1993, 1999; Hedger, 1990; Cairney, 1992, 2005; Rayner *et al.*, 1995; Boddy and Jones, 2006). Rhizomorphs are linear organs, with a thick melanized rind, the whole organ extending from the tip (Rayner *et al.*, 1985). Mycelial cords are also insulated from the environment with a thick rind, but they develop from a mycelial margin of diffuse hyphae, each of which extends apically. They can all draw on water, nutrients and energy held within other parts of the mycelium to sustain growth outside the organic resource(s) to which they are connected. In addition, although mycelial cords are insulated from the environment, they are able to absorb water and soluble nutrients via individual hyphae at the mycelial margin or that sometimes develop elsewhere, and they may colonize small litter components *en route* to large organic resources (Boddy, 1999; Watkinson *et al.*, 2006).

Fungi producing extra-resource mycelium risk loss of a large amount of biomass, as a result of invertebrate grazing, antagonistic microorganisms and death due to an unfavourable microenvironment, but this is minimized by a variety of different strategies. These include: (1) active growth and search for new resources; (2) a 'sit and wait' strategy, in which a mycelial network awaits arrival of resources, e.g. by branch fall, and then active colonization, often responding elsewhere in the system; and (3) most commonly, a combination of both. With all these strategies the mycelial networks are continuously remodelled in response to environmental cues, which can be abiotic (e.g. nutrient sources, microclimate or destructive events) and biotic (e.g. interaction with other fungi or grazing by invertebrates). Remodelling occurs through a complex combination of growth, branching, hyphal fusion and regression of different mycelial regions. Throughout the network, not only does morphology but also a complex set of physiological processes associated with uptake, storage and redistribution of nutrients change (Bebber *et al.*, 2006; Watkinson *et al.*, 2006). Both morphological and physiological changes are highly coordinated so that responses to local environmental changes can propagate through the mycelial network.

### 4.1 Search and Response Behaviour

Fungi have evolved a wide variety of patterns of mycelial outgrowth from resources into soil and litter (Figure 2; Boddy, 1999; Boddy and Jones, 2006). These have been quantified in terms of radial extension rate, hyphal coverage, and surface and mass fractal dimension ( $D_S$  and  $D_M$ , respectively) (Boddy, 1999; Boddy *et al.*, 1999; Boddy and Donnelly, 2007). These range between mycelia characterized by diffuse, slowly extending search fronts, with a high  $D_M$  (close to 2 in two dimensions), e.g. *H. fasciculare* (Figure 2b) and *Stropharia* spp., and open



**Figure 2** Patterns of Mycelial Outgrowth of Four Cord-Forming Basidiomycota across Compacted Soil in  $24 \times 24$  cm Trays from  $x$  cm (a–e) and  $y$  cm (f) Beech (*Fagus sylvatica*) Wood Inocula. (a) *Coprinus picaceus*, (b) *Hypholoma fasciculare*, (c) *Phallus impudicus*, (d) *Resinicium bicolor* and (e and f) *Phanerochaete velutina*. Digital Images (a)–(d) Courtesy Alaa Alawi, and Digital Images (e) and (f) from Photographs taken by Rory Bolton.

systems characterized by well-defined, rapidly extending cords throughout the system, with a lower  $D_M$  (between 1 and  $\sim 1.8$ ), e.g. *Agrocybe gibberosa*, *Coprinus picaceus*, *Phallus impudicus*, *P. velutina* and *Resinicium bicolor*. The former can be considered to be short-range foragers that are likely to be successful in discovering and exploiting abundant, relatively homogeneously distributed resources as they search areas intensively (Figure 2b), and the latter long-range foragers that would be less successful at capitalizing on relatively homogeneously supplied nutrients, but would successfully discover large, more sparsely distributed resources. Mycelial systems tend to become more open with time as they become larger ( $D_M$  decreases; Donnelly *et al.*, 1995; Boddy *et al.*, 1999; Figure 2a, c and d); patterns are modified by the quantity and quality of the resource from which the mycelium is extending (Bolton and Boddy, 1993; Donnelly and Boddy, 1997a; Boddy *et al.*, 1999; Zakaria and Boddy, 2002; Figure 2e and f), soil structure and nutrient status (Donnelly and Boddy, 1998; Boddy *et al.*, 1999; Zakaria and Boddy, 2002), microclimate (Donnelly and Boddy, 1997b; Owen, 1997; Wells *et al.*, 2001), interaction with mycelia of other species (Donnelly and Boddy, 2001) and invertebrate grazing (Kampichler *et al.*, 2004; Harold *et al.*, 2005; Bretherton *et al.*, 2006; Tordoff *et al.*, 2006; Wood *et al.*, 2006; Chapter 9).

When new resources are encountered the mycelium responds with dramatic changes in morphology (system architecture) and often with considerable reallocation of biomass. When the new resources are substantially larger than those

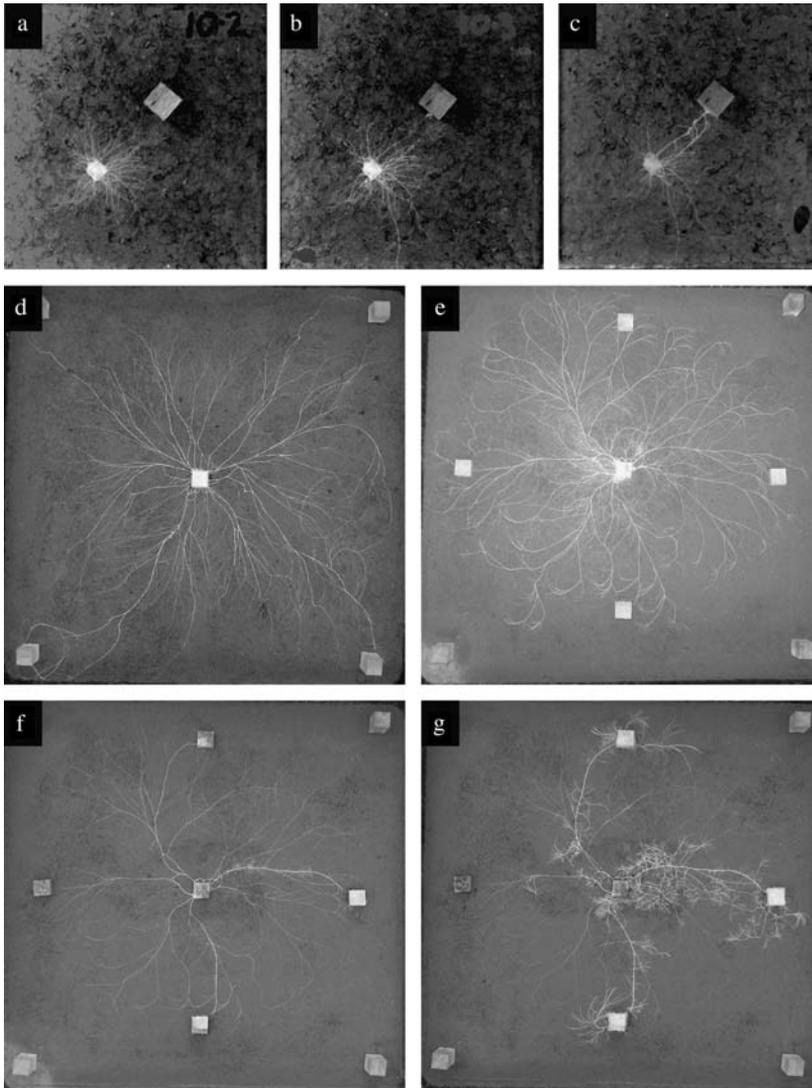
1 from which the mycelium emanated, mycelium connecting the new resource  
2 with the original resource usually aggregates to form thick cords, while radial  
3 extension slows or ceases, and non-resource-connected mycelium regresses  
(Dowson *et al.*, 1986, 1988; Bolton *et al.*, 1991; Boddy, 1993, 1999; Bolton, 1993;  
4 Donnelly and Boddy, 1997a; Figure 3a–c). Subsequently mycelium grows out  
5 from the newly colonized resource, and foraging continues, though the amount  
6 of time before foraging continues depends on the sizes of the original and new  
7 resource (Bolton, 1993; Boddy and Jones, 2006). With short-range foragers (e.g.  
8 *H. fasciculare*), there are similar, although less dramatic, changes to system  
9 architecture even when newly encountered resources are similar in size to the  
10 original resource.

11 Not only does the mycelium respond by changes to system architecture but  
12 also with physiological responses: there is highly coordinated uptake, storage  
13 and redistribution of nutrients throughout the network (Watkinson *et al.*, 2006;  
14 Chapter 3). Mineral nutrients (e.g. nitrogen and phosphorous) can be transported  
15 from wood resources to support growth at the mycelial margin, and nutrients  
16 scavenged as mycelia extend through soil can be translocated away from sites of  
17 uptake to sites of demand or storage, and commonly accumulate in wood  
18 resources connected within the mycelial system (Wells and Boddy, 1990; Wells  
19 *et al.*, 1990, 1997, 1998, 1999; Cairney, 1992). Rates of translocation can be rapid  
20 (sometimes  $> 25 \text{ cm h}^{-1}$ ), the largest fluxes being through cords interconnecting  
21 resources (e.g. Wells and Boddy, 1990). Many factors, including the overall  
22 nutritional status of the mycelial system, and the distribution and quantity of  
23 colonized and newly encountered organic resources, affect the balance between,  
24 and the main sites of, uptake, storage and demand for carbon and mineral  
25 nutrients (Abdalla and Boddy, 1996; Hughes and Boddy, 1996; Wells *et al.*, 1998,  
26 1999; Boddy and Jones, 2006).

## 27 4.2 Persistent Mycelial Networks: ‘Sit and Wait’ Strategy

28 Saprotrophic cord- and rhizomorph-forming Basidiomycota produce extensive  
29 long-lived mycelial networks on the forest floor, eventually covering several  
30 square metres to many hectares (Thompson and Rayner, 1982; Thompson and  
31 Boddy, 1988; Smith *et al.*, 1992; Ferguson *et al.*, 2003; Cairney, 2005; Figure 1e).  
32 The largest recorded to date is a genet of *Armillaria ostoyae* spanning 965 ha,  
33 with a maximum separation of 3,810 m and estimated as 1,900–8,650 years old  
34 (Ferguson *et al.*, 2003). The true extent and degree of connectivity within a genet  
35 is not known, however, since parts of mycelia can be separated from each other  
36 during development, and can also rejoin if parts of the same genet meet again.  
37 Similar systems are also found in the canopy of tropical forests where they  
38 effectively form a net (Hedger, 1990). Whether on the forest floor or in the canopy,  
39 these large, persistent networks allow capture of resources arriving by litter fall  
40 or root death at any time.

41 Although persistent, established systems are dynamic both as continued ex-  
42 tension at growing fronts (Thompson and Rayner, 1983) and as renewed mycelial  
43 growth from mature cords. Arrival of new resources can result in reallocation of  
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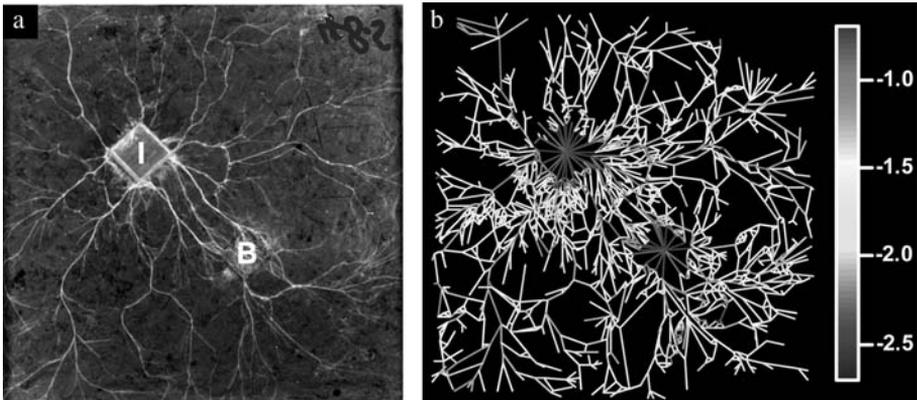
**Figure 3** Reallocation of Mycelial Biomass of *Phanerochaete velutina* following Colonization of New Wood Resources. (a–c) Extending from a 0.5 cm<sup>3</sup> Beech (*Fagus sylvatica*) Wood Inoculum to an 8 cm<sup>3</sup> Wood Resource, in 24 × 24 cm Trays of Non-Sterile Soil, after, respectively, 11, 15 and 20 Days. Note Regression of much of the Mycelium not Connected to a New Resource, and Thickening of Connected Cords (c). (d–g) Growth in 57 × 57 cm Soil Trays, with Four New Wood Resources (Located Half Way along each Microcosm Side) added after 36 Days in (e)–(g). (d) Control with No Additional Wood Resources. Images were Captured 78–85 Days after adding the Central Wood Inoculum. Note Thickening of Cords Connecting Inoculum with New Resources (f and g), and Thinning of Other Areas compared with 78 Days Control having No Additional Resources (e). Outgrowth from the Newly Colonized Lower Resource is Evident from 78 Days (Perspex Blocks in the Corners of Trays were for Support of Other Replicates in Stacks). Proliferation of Mycelium occurred along Cords linking the Central Wood Inoculum with New Resources between 78 Days (f) and 85 Days (g). Digital Images (a)–(c) from Photographs taken by Rory Bolton. Digital Images (d)–(g) Courtesy of Jon Wood.

1 biomass, with thickening of cords connecting resources, and regression of non-  
 3 connective fine mycelium (Wood *et al.*, 2006; Figure 3d–g). Moreover, sometimes  
 5 renewed growth occurs elsewhere as ephemeral patches of much branched fine  
 7 hyphae or along cords interconnecting new and original resources (Wells *et al.*,  
 9 1997; Wood *et al.*, 2006; Figure 3g). The patches have been shown, using  $^{32}\text{P}$   
 11 orthophosphate, to be sites of nutrient uptake (Wells *et al.*, 1977), and presumably  
 developed to satisfy the increased demand for nutrients to produce mycelial  
 biomass and enzymes during early stages of colonization and decomposition.  
 Carbon and mineral nutrients are continually rerouted to sites of need in mycelial  
 systems interconnecting a variety of resources in different states of decay (Wells  
*et al.*, 1998).

## 13 5. ANALYSIS OF NETWORK ARCHITECTURE AND FUNCTION

15 Within the mycelial networks of saprotrophic Basidiomycota there is consider-  
 17 able scope for communication, since hyphae maintain continuity with their  
 19 immediate ‘ancestors’ and if contact is made with neighbouring regions can  
 become connected via *de novo* formation of cross-links (anastomoses). This results  
 both radially and tangentially in systems with many connected loops (Figure 4).

21 The mycelium has evolved differently in different species resulting in a range  
 23 of network architectures, adapted differently for differing balances of explora-  
 25 tion, transport efficiency and resilience to damage. Highly interconnected my-  
 celia are costly to construct but offer alternate transport routes and thus resilience  
 to damage. Sparse networks with fewer interconnections can extend further for a



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 41 **Figure 4** (a) Mycelium of *Phanerochaete velutina* after 25 Days Growth from a  $4\text{ cm}^3$  Beech  
 Wood Inoculum (I) across a Tray ( $24 \times 24\text{ cm}$ ) of Compressed Non-Sterile Woodland Soil. The  
 Fungus has Met and Colonized a Second Wood Block (B). Digital Image Courtesy of Rory  
 43 Bolton. (b) The Digitized Network of the Same Mycelium Coloured by  $\log_{10}$  of Link Cross-  
 Sectional Area. The Number of Nodes  $V = 1,738$ , Links  $E = 2,617$  and the Number of Separate  
 45 Parts  $G = 1$ . The Number of Closed Loops (Cycles) in the Illustrated System is  $E - V + G = 880$ ,  
 and the Fraction of All Possible Cycles Present  $\alpha = 0.25$ .

1 given construction cost, but risk the loss of pathways should one part of the  
 2 network become damaged. Networks can vary not only in their connectedness  
 3 but also in the strength of their connections. Thick cords confer greater transport  
 4 capacity and resistance to breakage, but are more costly to produce. While these  
 5 concepts have been implicit in discussions of fungal foraging strategies and  
 6 fractal descriptions of mycelia, the architecture of mycelial networks has been  
 7 little explored until recently (Bebber *et al.*, 2006; Fricker and Bebber, in press;  
 8 Fricker *et al.*, 2007).

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## 11 5.1 Quantifying Network Characteristics

12  $D_M$  is a useful metric for comparing space filling by mycelia (Boddy and  
 13 Donnelly, 2007), but it only expresses a small fraction of the complex architecture  
 14 of mycelial systems. Tools for analysing networks are, however, emerging from  
 15 graph theory and statistical mechanics (Albert and Barabási, 2001; Strogatz, 2001;  
 16 Dorogovtsev and Mendes, 2002; Newman, 2003; Ottino, 2004; Amaral, in press),  
 17 that are applicable to mycelial networks (Bebber *et al.*, 2006, 2007; Fricker and  
 18 Bebber, in press; Fricker *et al.*, 2007), and have already proved valuable for  
 19 understanding the properties of many physical systems that can be described as  
 20 sets of connected entities, including biological networks such as protein–protein  
 21 interactions and food webs (Bork *et al.*, 2004; Dunne *et al.*, 2004).

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22 A network is simply a set of nodes, or vertices, connected by a set of links, or  
 23 edges. Weights, that define properties such as resistance to breakage or transport  
 24 capacity, can be associated with either nodes or links, or both. The nodes of a  
 25 fungal mycelium are the tips, branch points and fusions of hyphae or cords,  
 26 while the links are the hyphae or cords themselves. Various weights can be  
 27 assigned to the nodes and links. For example, the mass of a cord can be ap-  
 28 proximated by its volume, the length multiplied by the cross-sectional area.  
 29 Similarly, assuming that cords are composed of bundles of hyphae rather than  
 30 being hollow tubes, the resistance to flow could be a function of the length  
 31 divided by the cross-sectional area, i.e. long thin tubes have a greater resistance to  
 32 flow.

33 The properties of nodes are often defined by the links to which they are  
 34 connected. In the case of networks without link weights (the majority of examples  
 35 in the literature lack this information), the number of links per node (termed  
 36 degree  $k$ ) is often used to describe something about the connectedness of the  
 37 network. This measure is unlikely to be of interest in describing mycelial net-  
 38 works, as the majority of nodes will be of degree  $k = 3$  (the branches and fusions)  
 39 or 1 (the cord tips). Instead, the sum of link weights per node, known as the  
 40 node strength, is likely to be of greater interest. For example, calculating  
 41 the node strength for link cross-sectional area could indicate which nodes are  
 42 likely to be important in transport.

43 The number of nodes ( $V$ ), links ( $E$ ) and separate part  $G$ , known as discon-  
 44 nected components or subgraphs,  $G = 1$  (for an unbroken network), form  
 45 the network that can be used to calculate the number of closed loops (cycles) in  
 the network via the simple relation  $E - V + G$  (Figure 4). This cyclomatic number

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1 is extremely important, for it indicates the number of alternate pathways among  
3 points in the network that determine both the resilience to damage and the  
5 capability of parallel flow. The cyclomatic number is typically normalized to the  
maximum number possible for a network of a given size, allowing networks with  
differing numbers of nodes to be compared.

## 7 5.2 Modelling Transport

9 The fungal mycelium is essentially a transport network for nutrients, water and  
11 metabolites (Chapter 3). Modelling of transport in the mycelium has been at-  
tempted using various approaches, including partial differential equations and  
13 autonomous agents (Edelstein and Segel, 1983; Deutsch *et al.*, 1993). Since these  
methods ignore the network structure of the mycelium, greater insights can be  
15 obtained by taking an explicitly network-based approach into the analysis of  
transport. One way to achieve this is to calculate shortest path distances from  
17 each node to every other. If the effective physiological distance, or transport  
resistance, from one end of a cord to the other is modelled as the cord length  
19 divided by its cross-sectional area, the shortest path from one node to another  
will be the route with the smallest sum of these distances. The shortest path is  
21 therefore effectively the path of least resistance. Analysis of shortest paths of  
*P. velutina*, growing from wood blocks over soil, shows that the shortest paths  
23 from the wood blocks to other nodes of the fungus are smaller than they would  
be in a network with identical topology (i.e. number and location of links and  
25 nodes) but with uniform cord transport capacity (Bebber *et al.*, submitted). The  
fungus has therefore allocated resources to cords in a way that increases its  
27 transport efficiency. The only nodes for which the fungus is less efficient than in  
the randomized system are those at the periphery of the mycelium, where very  
29 fine hyphae are located (Figure 4). Here the fungus has optimized mycelial dis-  
tribution for searching for new resources rather than optimizing for transport.

31 The routes taken by shortest paths can reveal other aspects of network trans-  
port. For example, the importance of a node can be estimated by its betweenness  
33 centrality, which is the proportion of shortest paths that pass through that node  
(Freeman, 1977). The proportion of paths that pass through the node with the  
35 greatest betweenness centrality is the central point dominance. In fungal net-  
works, resources such as wood blocks usually have the greatest betweenness  
centrality.

37 The shortest path is usually only one of the several routes that could be taken  
from one node to another. Transport through a real network will often make use  
39 of these alternate routes, in the same way that electricity will flow through each  
of a set of resistors in parallel. Use of shortest paths to characterize transport  
41 necessarily ignores the importance of these parallel pathways through the net-  
work. Methods for solving current flow (e.g. Wu, 2004) through networks of  
43 electrical resistors can in principle be used to model flow through mycelial net-  
works, for example, by applying a voltage to the inoculum and grounding the  
45 hyphal tips. This may provide more realistic models of flow than simply using  
the shortest path.

### 1 5.3 Modelling Resilience

3 In nature, fungal mycelia are threatened by damage from physical disturbance  
5 and targeted attack by grazers such as Collembola (Chapter 9). Network archi-  
7 tecture plays an important role in resilience to damage, through both route  
9 redundancy and the probability of link breakage. Assuming a spatially random  
11 mode of attack, the probability of a link being attacked is proportional to its  
13 length. If, when attacked, the probability of link breakage is inversely propor-  
15 tional to its cross-sectional area, then the joint probability of a link being attacked  
17 and broken is proportional to length divided by cross-sectional area. The effect of  
19 attack on transport can be followed by examining the global efficiency, the sum of  
21 the reciprocals of all shortest paths, as the network disintegrates (Latora and  
23 Marchiori, 2001). Paths that are no longer traversable due to the formation of  
multiple disconnected components are infinitely long, and thus contribute zero to  
the global efficiency. Global efficiency therefore declines with increasing propor-  
tions of broken links. Another way of characterizing resilience is through the  
reachability, or availability, of a network (Ross and Harary, 1959). Reachability is  
the proportion of shortest paths that still exist (i.e. are not infinitely long).  
Reachability is one for a network that has not been fragmented (i.e. consists of  
one subgraph), since all nodes are mutually available. Reachability does not  
depend on path length and is therefore independent of the link breakage prob-  
ability function, whereas the efficiency will be greater if thick cords are less likely  
to break than thin ones.

25 Another way to measure resilience is to measure the proportion of the original  
27 network that remains connected to the wood block as increasing numbers of links  
29 are broken. In nature, disconnection from a food supply is likely to result in death  
31 of the disconnected part. When networks of *P. velutina* were tested against model  
33 networks with uniform link weights, more of the fungal network remained  
35 attached to the inoculum when a given proportion of links were broken (Bebber  
37 *et al.*, submitted). This demonstrated that the allocation of resources to cords not  
only increases transport efficiency, but also increases the resilience of the network  
to this kind of random attack. Inspection of network models that have been  
attacked in this way suggests that the secret to this increased resilience is the  
maintenance of a connected core structure as peripheral cords are broken. This  
pattern is intriguingly similar to that obtained in real networks after attack by  
certain species of Collembola (Chapter 9). Other mycophagous species may at-  
tack networks in other ways, depending, for example, on the size of their  
mouthparts.

39

### 41 5.4 Changes in Network Architecture over Time

43 As already mentioned, in peripheral regions cords are thin and at growing fronts  
45 hyphae are not aggregated, and therefore have high resistance to transport and  
long path lengths to the inoculum. As the network develops, some links become  
strengthened, such that the path lengths become dramatically shortened over  
time, while other links are removed, leading to an overall decrease in the material

1 cost density over time (Bebber *et al.*, submitted). The expectation would be that  
2 such strengthening would be accompanied by an increase in the overall construction  
3 cost of the network. However, thinning and removal of extraneous  
4 cords actually results in a decrease in the volume of material per unit area covered  
5 by the network (Bebber *et al.*, submitted). The mechanism by which certain  
6 cords are selected for reinforcement while others are broken down remains  
7 unknown. A possible conceptual model is one of Darwinian evolution, in which  
8 multiple cords are produced but only the 'fittest', in some sense, survive and  
9 produce further growth.

## 11 5.5 Future Research Direction

13 One of the most important avenues for further research will be the comparison of  
14 network structures and dynamics among the many different cord-forming fungal  
15 species. Like any organism, a fungus must partition limited resources among  
16 competing requirements. For example, a very dense, highly connected network  
17 might have high transport capacity and resilience to damage or attack because of  
18 multiple transport pathways. However, it would incur a large material cost of  
19 construction per unit area of explored space, and would cover new ground  
20 slowly. Conversely, a sparse system could extend further for the same material  
21 cost, but would have fewer alternate routes and therefore lower resilience to  
22 disconnection. Variation in these tradeoffs among species could reveal important  
23 axes of niche differentiation in fungi.

24 Further, fungi provide one of the few real network systems that can be ex-  
25 perimentally manipulated, and that can actually rebuild themselves following  
26 damage. Analyses of cord-forming Basidiomycota mycelial systems are therefore  
27 likely to reveal a range of evolutionary solutions to network design that may  
28 inform the development of other types of transport network, e.g. road, rail and  
29 telephone.

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## 41 REFERENCES

- 43 Abdalla, S.H.M. and Boddy, L. (1996). Effect of soil and litter type on outgrowth patterns of mycelial  
44 systems of *Phanerochaete velutina*. *FEMS Microbiology Ecology*, **20**, 195–204.
- 45 Albert, R. and Barabási, A.-L. (2001). Statistical mechanics of complex networks. *Reviews of Modern  
46 Physics*, **74**, 47–97.

- 1 Amaral, L.A.N. and Ottino, J.M. (2004). Complex networks: Augmenting the framework for the study  
of complex systems. *European Physical Journal B*, **38**, 147–162.
- 3 Bebber, D.P., Tlalka, M., Hynes, J., Darrah, P.R., Ashford, A., Watkinson, S.C., Boddy, L. and  
Fricker, M.D. (2006). Imaging complex nutrient dynamics in mycelial networks. In: *Fungi and  
the Environment* (G.M. Gadd, S.C. Watkinson and P. Dyer, eds.), pp. 1–21. Cambridge University  
5 Press.
- 7 Bevercombe, G.P. and Rayner, A.D.M. (1980). Diamond bark disease of sycamore in Britain. *New  
Phytologist*, **86**, 379–392.
- 9 Boddy, L. (1984). The micro-environment of basidiomycete mycelia in temperate deciduous wood-  
lands. In: *Ecology and Physiology of the Fungal Mycelium* (D.H. Jennings and A.D.M. Rayner, eds.),  
pp. 261–289. Cambridge University Press.
- 11 Boddy, L. (1993). Saprotrophic cord-forming fungi: Warfare strategies and other ecological aspects.  
*Mycological Research*, **97**, 641–655.
- 13 Boddy, L. (1999). Saprotrophic cord-forming fungi: Meeting the challenge of heterogeneous environ-  
ments. *Mycologia*, **91**, 13–32.
- 15 Boddy, L. (2001). Fungal community ecology and wood decomposition processes: From standing tree  
to complete decay of coarse woody debris. In: *Ecology of Woody Debris in Boreal Forests*  
(B.G. Jonsson and N. Kruys, eds.), *Ecological Bulletins*, **49**, 43–56.
- 17 Boddy, L. and Donnelly, D.P. (2007). Fractal geometry and microorganisms in the environment. In:  
*Biophysical Chemistry of Fractal Structures and Process in Environmental Systems* (N. Senesi and  
K. Wilkinson, eds.). Wiley, in press.
- 19 Boddy, L. and Jones, T.H. (2006). Mycelial responses in heterogeneous environments: Parallels with  
macroorganisms. In: *Fungi in the Environment* (G.M. Gadd, S.C. Watkinson and P. Dyer, eds.),  
pp. 112–140. Cambridge University Press.
- 21 Boddy, L., Wells, J.M., Culshaw, C. and Donnelly, D.P. (1999). Fractal analysis in studies of mycelium in  
soil. *Geoderma*, **88**, 301–328.
- 23 Bolton, R.G. (1993). Resource acquisition by migratory mycelial cord systems of *Phanerochaete velutina*  
and *Hypholoma fasciculare*, PhD Thesis, University of Wales, Cardiff.
- 25 Bolton, R.G. and Boddy, L. (1993). Characterisation of the spatial aspects of foraging mycelial cord  
systems using fractal geometry. *Mycological Research*, **97**, 762–768.
- 27 Bolton, R.G., Morris, C.W. and Boddy, L. (1991). Non-destructive quantification of growth and  
regression of mycelial cords using image analysis. *Binary*, **3**, 127–132.
- 29 Bork, P., Jensen, L.J., Von Mering, C., Ramani, A.K., Lee, I. and Marcotte, E.M. (2004). Protein  
interaction networks from yeast to human. *Current Opinion in Structural Biology*, **14**, 292–299.
- 31 Bretherton, S., Tordoff, G.M., Jones, T.H. and Boddy, L. (2006). Compensatory growth of *Phanerochaete  
velutina* mycelial systems grazed by *Folsomia candida* (Collembola). *FEMS Microbiology Ecology*, **58**,  
33–44.
- 33 Cairney, J.W.G. (1992). Translocation of solutes in ectomycorrhizal and saprotrophic rhizomorphs.  
*Mycological Research*, **96**, 135–141.
- 35 Cairney, J.W.G. (2005). Basidiomycete mycelia in forest soils: Dimensions, dynamics and roles in  
nutrient distribution. *Mycological Research*, **109**, 7–20.
- 37 Deusch, A., Dress, A. and Rensing, L. (1993). Formation of morphological differentiation patterns in  
the ascomycete *Neurospora crassa*. *Mechanisms of Development*, **44**, 17–31.
- 39 Donnelly, D.P. and Boddy, L. (1997a). Resource acquisition by the mycelial-cord-former *Stropharia  
caerulea*: Effect of resource quantity and quality. *FEMS Microbiology Ecology*, **23**, 195–205.
- 41 Donnelly, D.P. and Boddy, L. (1997b). Development of mycelial systems of *Stropharia caerulea* and  
*Phanerochaete velutina* on soil: Effect of temperature and water potential. *Mycological Research*, **101**,  
705–713.
- 43 Donnelly, D.P. and Boddy, L. (1998). Developmental and morphological responses of mycelial systems  
of *Stropharia caerulea* and *Phanerochaete velutina* to soil nutrient enrichment. *New Phytologist*, **138**,  
519–531.
- 45 Donnelly, D.P. and Boddy, L. (2001). Mycelial dynamics during interactions between *Stropharia caerulea*  
and other cord-forming, saprotrophic basidiomycetes. *New Phytologist*, **151**, 691–704.

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- 1 Donnelly, D.P., Wilkins, M.F. and Boddy, L. (1995). An integrated image analysis approach for  
determining biomass, radial extent and box-count fractal dimension of macroscopic mycelial  
3 systems. *Binary*, **7**, 19–28.
- Dorogovtsev, S.N. and Mendes, J.F.F. (2002). Evolution of networks. *Advances in Physics*, **51**, 1079–1187.
- 5 Dowson, C.G., Rayner, A.D.M. and Boddy, L. (1986). Outgrowth patterns of mycelial cord-forming  
basidiomycetes from and between woody resource units in soil. *Journal of General Microbiology*,  
**132**, 203–211.
- 7 Dowson, C.G., Rayner, A.D.M. and Boddy, L. (1988). Foraging patterns of *Phallus impudicus*,  
*Phanerochaete laevis* and *Steccherinum fimbriatum* between discontinuous resource units in soil.  
*FEMS Microbiology Ecology*, **53**, 291–298.
- 9 Dowson, C.G., Rayner, A.D.M. and Boddy, L. (1989). Spatial dynamics and interactions of the wood-  
land fairy ring fungus, *Clitocybe nebularis*. *New Phytologist*, **111**, 699–705.
- 11 Dunne, J.A., Williams, R.J. and Martinez, N.D. (2004). Food-web structure and network theory: The  
role of connectance and size. *Proceedings of the National Academy of Sciences of the United States of  
13 America*, **99**, 12917–12922.
- Edelstein, L. and Segel, L.A. (1983). Growth and metabolism of mycelial fungi. *Journal of Theoretical  
15 Biology*, **104**, 187–210.
- Ferguson, B.A., Dreisbach, T.A., Parks, C.G., Filipo, G.M. and Schmitt, C.L. (2003). Coarse-scale pop-  
17 ulation structure of pathogenic *Armillaria* species in a mixed-conifer forest in the Blue Mountains  
of northeast Oregon. *Canadian Journal of Forest Research*, **33**, 612–623.
- Freeman, L.C. (1977). A set of measures of centrality based on betweenness. *Sociometry*, **40**, 35–41.
- 19 Fricker, M.D. and Bebbler, D.P. Network organization of mycelial fungi. *The Mycota*, in press.
- Fricker, M.D., Bebbler, D., Darrah, P.R., Tlalka, M., Watkinson, S.C., Boddy, L., Yiasoumis, L., Cartwright,  
21 H.M., Meškauskas, A., Moore, D., Smith, M.D., Nakagaki, T., Lee, C.F. and Johnson, N. (2007).  
Inspiration from microbes: From patterns to networks. In: *Complex Systems and Inter-Disciplinary  
23 Science* (B.W. Arthur, R. Axtell, S. Bornholdt, J. Efstathiou, P.M. Hui, P. Maini, M. Nowak,  
R. Sole, D. Stauffer, F. Reed-Tsochas and K. Turner, eds.). World Scientific Publishing Co., London,  
in press.
- 25 Harold, S., Tordoff, G.M., Jones, T.H. and Boddy, L. (2005). Mycelial responses of *Hypholoma fasciculare*  
to collembola grazing: Effect of inoculum age, nutrient status and resource quality. *Mycological  
Research*, **109**, 927–935.
- 27 Hedger, J. (1990). Fungi in the tropical forest canopy. *The Mycologist*, **4**, 200–202.
- Hughes, C.L. and Boddy, L. (1994). Translocation of  $^{32}\text{P}$  between wood resources recently colonised by  
29 mycelial cord systems of *Phanerochaete velutina*. *FEMS Microbiology Ecology*, **14**, 201–212.
- Hughes, C.L. and Boddy, L. (1996). Sequential encounter of wood resources by mycelial cords of  
31 *Phanerochaete velutina*: Effect on growth patterns and phosphorus allocation. *New Phytologist*, **133**,  
713–726.
- Kampichler, C., Rolschewski, J., Donnelly, D.P. and Boddy, L. (2004). Collembolan grazing affects the  
33 growth strategy of the cord-forming fungus *Hypholoma fasciculare*. *Soil Biology and Biochemistry*, **36**,  
591–599.
- Latora, V. and Marchiori, M. (2001). Efficient behaviour of small-world networks. *Physical Review  
35 Letters*, **87**, 198701-1–198701-4.
- Newman, M.E.J. (2003). The structure and function of complex networks. *SIAM Review*, **45**,  
37 167–256.
- Olsson, S. and Gray, S.N. (1998). Patterns and dynamics of  $^{32}\text{P}$  phosphate and  $^{14}\text{C}$  labelled AIB  
39 translocation in intact basidiomycete mycelia. *FEMS Microbiology Ecology*, **26**, 109–120.
- Owen, S.L. (1997). Comparative development of the mycelial cord-forming fungi *Coprinus picaceus* and  
41 *Phanerochaete velutina*, with particular emphasis on pH and nutrient reallocation, PhD Thesis,  
University of Wales, Cardiff.
- Rayner, A.D.M. and Boddy, L. (1988). *Decomposition of Wood: Its Biology and Ecology*. Wiley, Chichester,  
43 UK.
- Rayner, A.D.M., Griffith, G.S. and Ainsworth, A.M. (1995). Mycelia interconnectedness. In: *The Grow-  
45 ing Fungus* (N.A.R. Gow and G.M. Gadd, eds.), pp. 21–40. Chapman and Hall, London.

- 1 Rayner, A.D.M., Powell, K.A., Thompson, W. and Jennings, D.H. (1985). Morphogenesis of vegetative  
organs. In: *Developmental Biology of Higher Fungi* (D. Moore, L.A. Casselton, D.A. Wood and  
3 J.C. Frankland, eds.), pp. 249–279. Cambridge University Press.
- Ross, I.C. and Harary, F. (1959). A description of strengthening and weakening members of a group.  
5 *Sociometry*, **22**, 139–147.
- Smith, M.L., Bruhn, J.N. and Anderson, J.B. (1992). The fungus *Armillaria bulbosa* is among the largest  
and oldest living organisms. *Nature*, **356**, 428–431.
- 7 Strogatz, S.H. (2001). Exploring complex networks. *Nature*, **410**, 268–276.
- Thompson, W. and Boddy, L. (1988). Decomposition of suppressed oak trees in even-aged plantations.  
II. Colonisation of tree roots by cord and rhizomorph producing basidiomycetes. *New Phytologist*,  
9 **93**, 277–291.
- Thompson, W. and Rayner, A.D.M. (1982). Spatial structure of a population of *Tricholomopsis*  
11 *platyphylla* in a woodland site. *New Phytologist*, **92**, 103–114.
- Thompson, W. and Rayner, A.D.M. (1983). Extent development and functioning of mycelial cord  
13 systems in soil. *Transactions of the British Mycological Society*, **81**, 333–345.
- Tordoff, G.M., Jones, T.H. and Boddy, L. (2006). Grazing by *Folsomia candida* (Collembola) affects the  
15 mycelial morphology of the cord-forming basidiomycetes *Hypholoma fasciculare*, *Phanerochaete*  
*velutina* and *Resinicium bicolor* differently during early outgrowth onto soil. *Mycological Research*,  
**110**, 335–345.
- 17 Watkinson, S.C., Bebber, D., Darrah, P., Fricker, M., Tlalka, M. and Boddy, L. (2006). The role of wood  
decay fungi in the carbon and nitrogen dynamics of the forest floor. In: *Fungi in Biogeochemical*  
*Cycles* (G.M. Gadd, ed.), pp. 151–181. Cambridge University Press.
- 19 Wells, J.M. and Boddy, L. (1990). Wood decay, and phosphorus and fungal biomass allocation, in  
mycelial cord systems. *New Phytologist*, **116**, 285–295.
- 21 Wells, J.M., Donnelly, D.P. and Boddy, L. (1997). Patch formation and developmental polarity in  
mycelial cord systems of *Phanerochaete velutina* on nutrient-depleted soil. *New Phytologist*, **136**,  
23 653–665.
- Wells, J.M., Harris, M.J. and Boddy, L. (1998). Temporary phosphorus partitioning in mycelial systems  
of the cord-forming basidiomycete *Phanerochaete velutina*. *New Phytologist*, **140**, 283–293.
- 25 Wells, J.M., Harris, M.J. and Boddy, L. (1999). Dynamics of mycelial growth and phosphorus par-  
titioning in developing *Phanerochaete velutina*: Dependence on carbon availability. *New Phytologist*,  
27 **142**, 325–334.
- Wells, J.M., Hughes, C. and Boddy, L. (1990). The fate of soil-derived phosphorus in mycelial cord  
29 systems of *Phanerochaete velutina* and *Phallus impudicus*. *New Phytologist*, **114**, 595–606.
- Wells, J.M., Thomas, J. and Boddy, L. (2001). Soil water potential shifts: Developmental responses  
and dependence on phosphorus translocation by the cord-forming basidiomycete *Phanerochaete*  
31 *velutina*. *Mycological Research*, **105**, 859–867.
- Wood, J., Tordoff, G.M., Jones, T.H. and Boddy, L. (2006). Reorganization of mycelial networks of  
33 *Phanerochaete velutina* in response to new woody resources and collembola grazing. *Mycological*  
*Research*, **110**, 985–993.
- 35 Wu, F.Y. (2004). Theory of resistor networks: The two-point resistance. *Journal of Physics A*, **37**,  
6653–6673.
- 37 Zakaria, A.J. and Boddy, L. (2002). Mycelial foraging by *Resinicium bicolor*: Interactive effects of  
resource quantity, quality and soil composition. *FEMS Microbiology Ecology*, **40**, 135–142.
- 39
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- 43
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